# Guangzhou Discrete Mathematics Seminar 

# Graphs with girth 9 and without <br> longer odd holes are 3-colorable 

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For a number $l \geq 2$, let $\mathcal{G}_{l}$ denote the family of graphs which have girth $2 l+1$ and have no odd hole with length greater than $2 l+1$. Wu, Xu and Xu conjectured that every graph in $\bigcup_{l \geq 2} \mathcal{G}_{l}$ is 3 -colorable. Chudnovsky et al., Wu et al., and Chen showed that every graph in $\mathcal{G}_{2}, \mathcal{G}_{3}$ and $\bigcup_{l \geq 5} \mathcal{G}_{l}$ is 3 -colorable respectively. In this paper, we prove that every graph in $\mathcal{G}_{4}$ is 3 -colorable. This confirms Wu, Xu and Xu's conjecture.

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